

Shielding from Space Radiations

Annual Technical Report

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Period: December 1, 1992 through June 1, 1993

**CHRISTOPHER NEWPORT UNIVERSITY
NEWPORT NEWS, VIRGINIA 23606-2998**

NASA GRANT NUMBER 1-1286

December 1, 1993

(NASA-CR-194664) SHIELDING FROM
SPACE RADIATIONS Annual Progress
Report, 1 Dec. 1992 - 1 Jun. 1993
(Christopher Newport Coll.) 39 p

N94-17255

Unclass

G3/93 0193164

ABSTRACT

This Progress Report covering the period of June 1, 1993 to December 1, 1993 presents the development of an analytical solution to the heavy ion transport equation in terms of a one-layer Green's function formalism. The mathematical developments are recasted into an efficient computer code for space applications. The efficiency of this algorithm is accomplished by a nonperturbative technique of extending the Green's function over the solution domain. The code may also be applied to accelerator boundary conditions to allow code validation in laboratory experiments. Results from the isotopic version of the code with 80 isotopes present for a single layer target material, for the case of an Iron beam projectile at 600 MeV/nucleon in water is presented.

INTRODUCTION

Future NASA missions will be limited by exposure to space radiations unless adequate shielding is provided to protect men and equipments from such radiations. Adequate methods required to estimate the damage caused by such radiations behind various shields can be evaluated prior to commitment to such missions.

From the inception of the Langley Research Center heavy ion (HZE) shielding program (refs. 1-3), there has been a continued, close relationship between code development and laboratory experiment (ref. 3). Indeed, the current research goal is to provide computationally efficient high charge and energy ion (HZE) transport codes which can be validated with laboratory experiments and subsequently applied to space engineering design. In practice, two streams of code development have prevailed due to the strong energy dependence of necessary atomic/molecular cross sections and the near singular nature of the laboratory beam boundary conditions (refs. 4-6). The atomic/molecular cross section dependence is adequately dealt with by using the methods of Wilson and Lamkin (ref. 7), allowing efficient numerical procedures to be developed for space radiations (refs. 6,8-10). Although these codes could conceivably be applied to the laboratory validation, methods to control truncation and discretization errors would bear little resemblance to the space radiation codes attempting to be validated. Clearly, a radical reorientation is required to achieve the validation goals of the current NASA space radiation shielding program, and such an approach is the main thrust of this research and is briefly described below.

A useful technique in space radiation shielding is the use of the impulse response Green's function (refs. 11,12), which satisfies the Boltzman equation of the form

$$\left[\vec{\Omega} \cdot \vec{\nabla} - \frac{\partial}{\partial E} \tilde{S}_j(E) + \sigma_j \right] G_{jm}(E, E_o, \vec{\Omega}, \vec{x}) \\ = \sum_k \int \sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}') G_{km}(E', E_o, \vec{\Omega}', \vec{x}) d\vec{\Omega}' dE' \quad (1)$$

where G_{jm} reduces to a monoenergetic unidirectional function at the boundary, $\tilde{S}_j(E)$ is the stopping power, σ_j is the total cross section, and σ_{jk} is the inclusive differential cross section. An arbitrary solution to the Boltzman equation within a closed convex region can be written as

$$\phi_j(E, \vec{\Omega}, \vec{x}) = \sum_m \int G_{jm}(E, E', \vec{\Omega} - \vec{\Omega}', \vec{x} - \vec{\Gamma}) \\ \times f_m(E', \vec{\Omega}', \vec{\Gamma}) d\vec{\Omega}' dE' d\vec{\Gamma} \quad (2)$$

where $f_m(E', \vec{\Omega}', \vec{\Gamma})$ is the incident flux at the boundary (ref. 11). Since transport problem is formulated in terms of a single Green's function algorithm, the validation of the Green's function in the laboratory meets the objective of having a space validated code. Since there is hope of a Green's function based on an analytical solution of the Boltzmann equation (ref. 13), the resulting evaluation of the shield properties should be computationally efficient.

The first step in this process is to develop an equivalent Green's function algorithm in one dimension to match the current capability in space radiation transport calculation (refs. 6,14). The algorithm is based on the closed form solution to the one dimensional equation

$$\left(\frac{\partial}{\partial x} - \frac{\partial}{\partial E} \bar{S}_j(E) + \sigma_j \right) G_{jm}(E, E_0, x) \\ = \sum_k \int \sigma_{jk}(E, E') G_{km}(E', E_0, x) dE' \quad (3)$$

for a monoenergetic beam at the boundary. The probability of validation for ²⁰Ne beams of this algorithm (with multiple scattering corrections) has already shown good correlation (refs. 5,15), but improvements in the nuclear data base are required for achieving higher correlations with experiment. If considerations are restricted to multiple charged ions then the right hand side of equation (3) can be further reduced to

$$\left[\frac{\partial}{\partial x} - \frac{\partial}{\partial E} \bar{S}_j(E) + \sigma_j \right] G_{jm}(E, E_0, x) \\ = \sum_k \sigma_{jk} G_{km}(E, E_0, x) \quad (4)$$

for which a solution is presented below.

APPROXIMATE GREENS'S FUNCTION

Equation (4) can be simplified by transforming the energy into the the residual range as

$$r_j = \int_0^E dE' / \bar{S}_j(E') \quad (5)$$

and defining new field variables as

$$\psi_j(x, r_j) = \bar{S}_j(E) \phi_j(x, E) \quad (6)$$

$$G_{jm}(x, r_j, r'_m) = \bar{S}_j(E) G_{jm}(x, E, E') \quad (7)$$

so that equation (4) becomes

$$\left[\frac{\partial}{\partial x} - \frac{\partial}{\partial r_j} + \sigma_j \right] g_{jm}(x, r_j, r'_m) \\ = \sum_k \frac{\nu_j}{\nu_k} \sigma_{jk} g_{km}(x, r_j, r'_m) \quad (8)$$

with boundary condition

$$g_{jm}(0, r_j, r'_m) = \delta_{jm} \delta(r_j - r'_m) \quad (9)$$

and

$$\psi_j(x, r_j) = \sum_m \int_0^\infty g_{jm}(x, r_j, r'_m) f_m(r'_m) dr'_m \quad (10)$$

The solution to equation (8) may be written as

$$g_{jm}(x, r_j, r'_m) = \sum_i g_{jm}^{(i)}(x, r_j, r'_m) \quad (11)$$

where zeroth order term of equation (11) is

$$g_{jm}^{(0)}(x, r_j, r'_m) = g(j) \delta_{jm} \delta(x + r_j - r'_m) \quad (12)$$

and the first order term of equation (11) is

$$g_{jm}^{(1)}(x, r_j, r'_m) \approx \frac{\nu_j \sigma_{jm} g(j, m)}{x(\nu_m - \nu_j)} \quad (13)$$

with the condition that $g_{jm}^{(1)}(x, r_j, r'_m)$ is zero unless

$$\frac{\nu_j}{\nu_m} (r_j + x) \leq r'_m \leq \frac{\nu_i}{\nu_m} r_j + x \quad (14)$$

The second order terms of equation (11) are

$$g_{jm}^{(2)}(x, r_j, r'_m) \approx \sum_k \frac{\sigma_{jk} \sigma_{km} g(j, k, m)}{r'_{mu} - r'_{ml}} \quad (15)$$

with the condition that $g_{jm}^{(2)}(x, r_j, r'_m)$ are nonzero for

$$r'_{m\ell} \leq r'_m \leq r'_{mu} \quad (16)$$

where

$$r'_{mu} = \left\{ \begin{array}{ll} \frac{\nu_j}{\nu_m} r_j + x & (\nu_m > \nu_k > \nu_j) \\ \frac{\nu_j r_j + \nu_k x}{\nu_m} & (\nu_k > \nu_m > \nu_j) \\ \frac{\nu_j}{\nu_m} r_j + x & (\nu_m > \nu_j > \nu_k) \end{array} \right\} \quad (17)$$

and

$$r'_{m\ell} = \left\{ \begin{array}{ll} \frac{\nu_j}{\nu_m} (r_j + x) & (\nu_m > \nu_k > \nu_j) \\ \frac{\nu_j}{\nu_m} (r_j + x) & (\nu_k > \nu_m > \nu_j) \\ \frac{\nu_j r_j + \nu_k x}{\nu_m} & (\nu_m > \nu_j > \nu_k) \end{array} \right\} \quad (18)$$

The third order terms of equation (11) are

$$g_{jm}^{(3)}(x, r_j, r'_m) \approx \sum_{k, \ell} \frac{\sigma_{jk} \sigma_{k\ell} \sigma_{\ell m} g(j, k, \ell, m)}{r'_{mu} - r'_{m\ell}} \quad (19)$$

and similarly for higher order terms. In the above the g 's of n arguments are given by

$$g(j) = e^{-\sigma_j x} \quad (20)$$

and

$$\begin{aligned} &g(j_1, j_2, \dots, j_n, j_{n+1}) \\ &= \frac{g(j_1, j_2, \dots, j_{n-1}, j_n) - g(j_1, j_2, \dots, j_{n-1}, j_{n+1})}{\sigma_{j_{n+1}} - \sigma_{j_n}} \end{aligned} \quad (21)$$

In terms of above, the solution to equation (4) may be written as

$$\begin{aligned} \psi_j(x, r_j) = & e^{-\sigma_j x} f_j[R_j^{-1}(r_j + x)] \\ & + \sum_{m,i} G_{jm}^{(i)}(x) \left\{ F_m[R_m^{-1}(r'_{m\ell})] \right. \\ & \left. - F_m[R_m^{-1}(r'_{mu})] \right\} \end{aligned} \quad (22)$$

where

$$G_{jm}^{(i)}(x) = \sum_{j_1, j_2, \dots, j_{n-2}} \frac{\sigma_{jj_1} \sigma_{j_1 j_2} \dots \sigma_{j_{n-2} m} g(j, j_1 j_2 \dots j_{n-2}, m)}{\Delta^{(i)}} \quad (23)$$

for $i=1$, the denominator of equation (23) is

$$\Delta^{(1)} = x \left(\frac{\nu_m}{\nu_j} - 1 \right) \quad (24)$$

and for $i>1$, the denominator becomes

$$\Delta^{(i)} = \begin{cases} x \left(1 - \frac{\nu_j}{\nu_m} \right) & (\nu_m > \nu_k > \nu_j) \\ x \left(\frac{\nu_k}{\nu_m} - \frac{\nu_j}{\nu_m} \right) & (\nu_k > \nu_m > \nu_j) \\ x \left(1 - \frac{\nu_k}{\nu_m} \right) & (\nu_m > \nu_j > \nu_k) \end{cases} \quad (25)$$

In equation (22), $F_m(E)$ is the integral flux at the boundary, and is defined as

$$F_m(E) = \int_E^{\infty} f_m(E') dE' \quad (26)$$

Implementation of equation (22) can now be accomplished independent of the character of the boundary values $f_m(E')$ and will give accurate results for both space and laboratory applications.

DISCUSSION OF RESULTS

Values of collision related fluxes for 3 depths of water target for a mono-energetic beam of Iron projectile with 600 MeV/nucleon are shown in figures 1 through 3 for both the perturbative and nonperturbative Green's function methods for the direct comparison of the two methods. The first three collision terms and the sum of all collision terms of both theories at a depth of 5 cm of water are shown in figure 1.A through 1.H. The differences in the spectral shape is due to the simplification of the attenuation term in the nonperturbative theory. The nonperturbation terms represent the average spectrum while perturbation theory retains the spectral shape. Figures 2.A through 2.H and 3.A through 3.H are the corresponding comparison of the two methods at depths of 10 and 15 cm of water. Direct comparisons of figures 1 through 3 shows that the sequence of perturbation terms appear to be converging to a result similar to that of nonperturbative result.

The main advantage of nonperturbative methods are in their computational efficiencies. The computational time required for the nonperturbative code is about 10 minutes on VAX 4000 compared to 15, 45, 90 minutes for the 1-st, 2-nd and 3-rd collision terms of the perturbation solution.

Figures 4.A through 4.C show the corresponding differential LET spectrum using the method of reference 16. The highest LET peak is due to the primary beam and the ion fragments. The successive peaks below iron are due to lower atomic weight fragments. Such LET spectra can be compared to experimental measurements directly.

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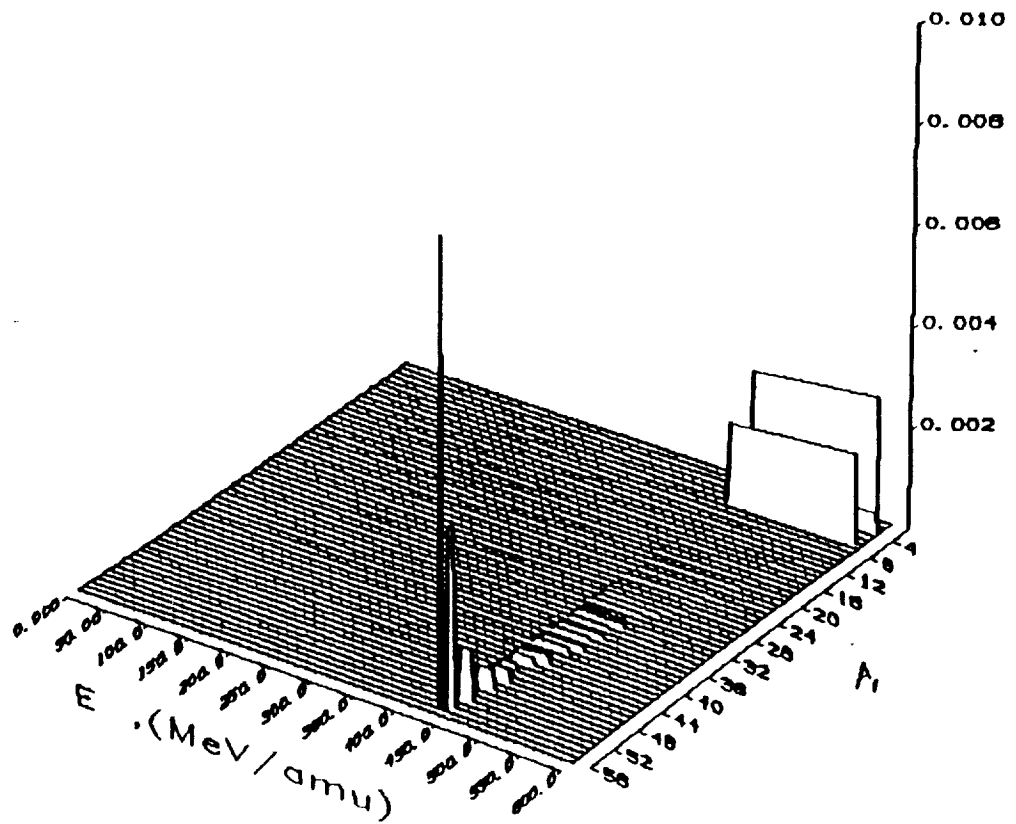


Figure 1.A. 1-st term nonperturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

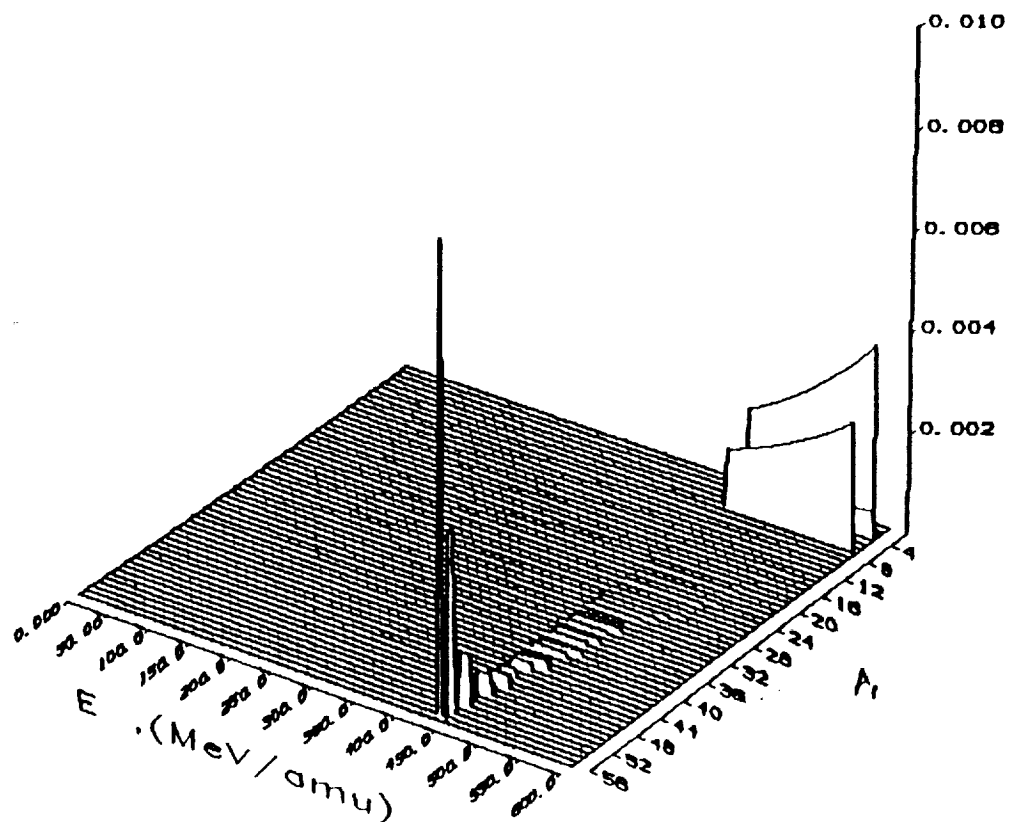


Figure 1.B. 1-st term perturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

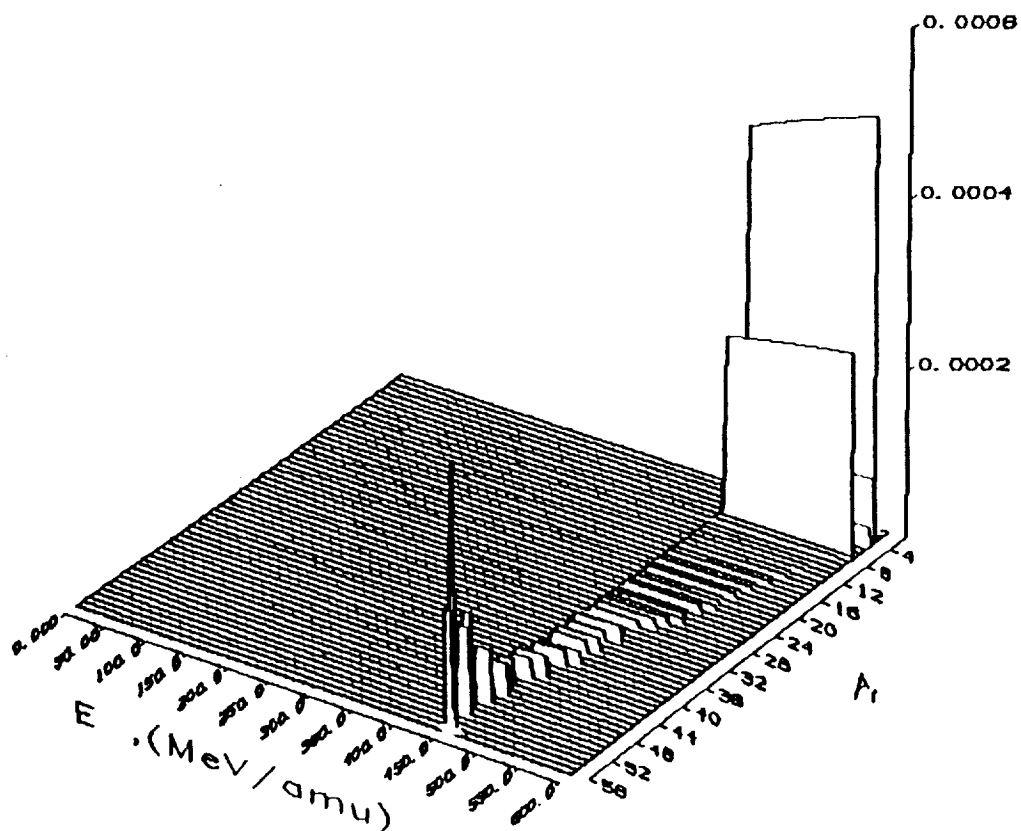


Figure 1.C. 2-nd term nonperturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

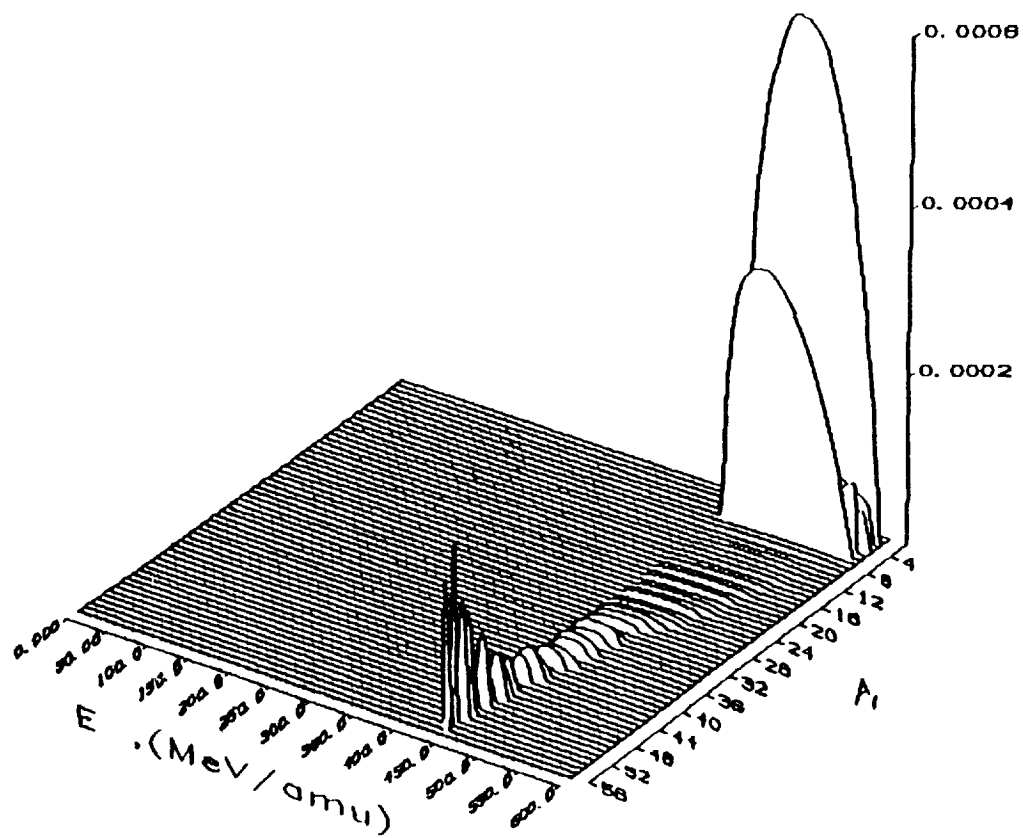


Figure 1.D. 2-nd term perturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

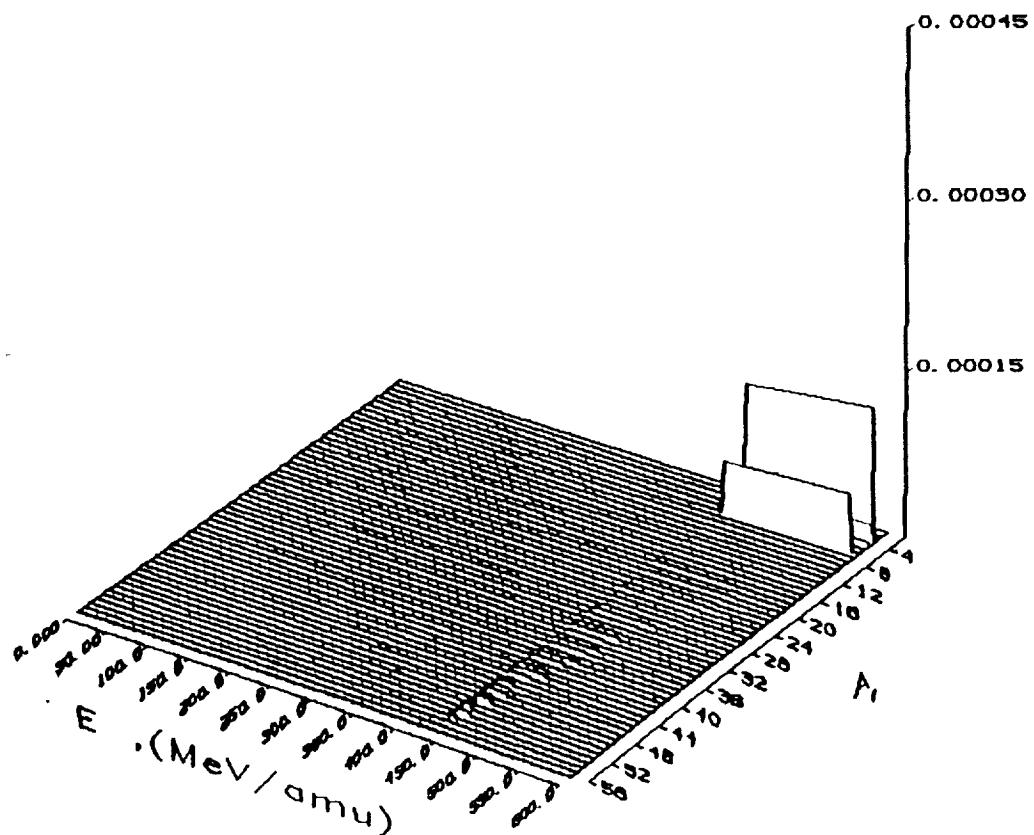


Figure 1.E. 3-rd term nonperturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

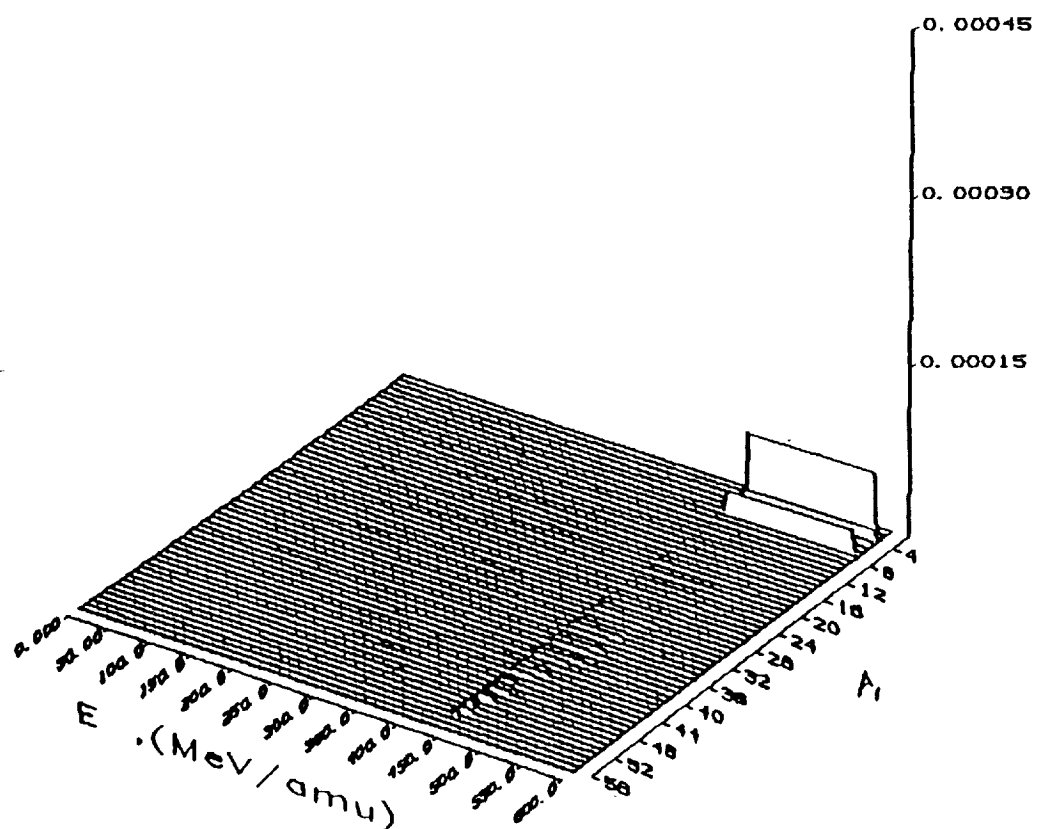


Figure 1.F. 3-rd term perturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

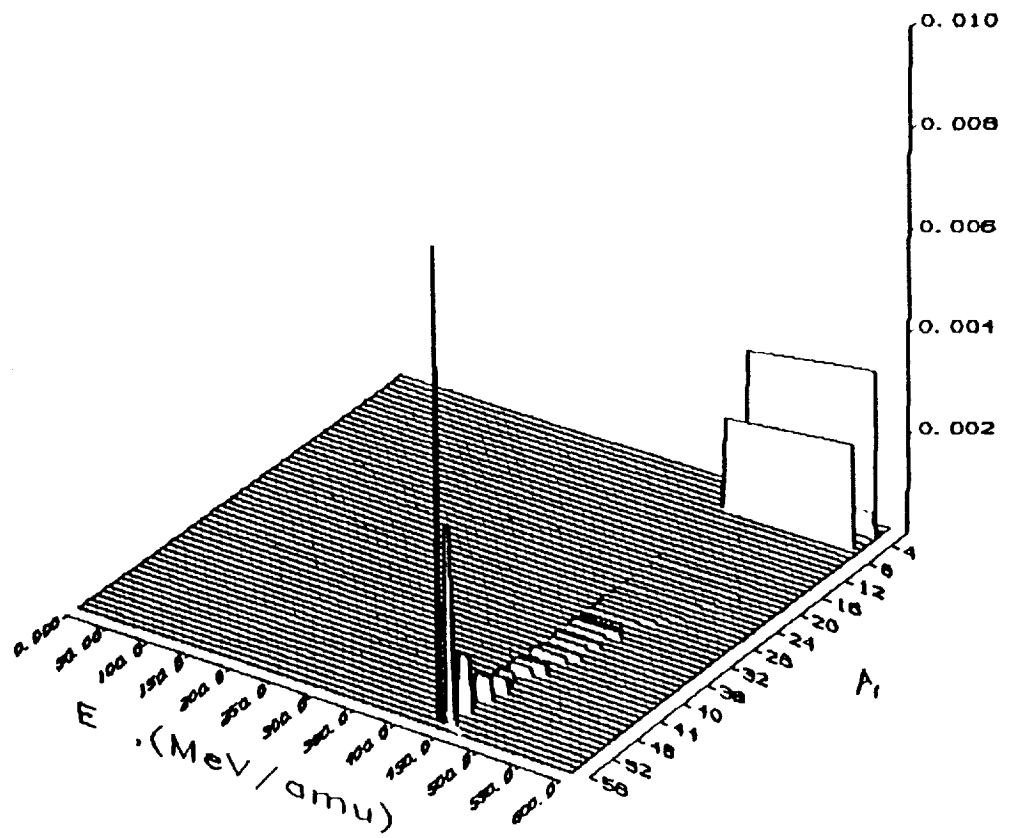


Figure 1.G. All terms nonperturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

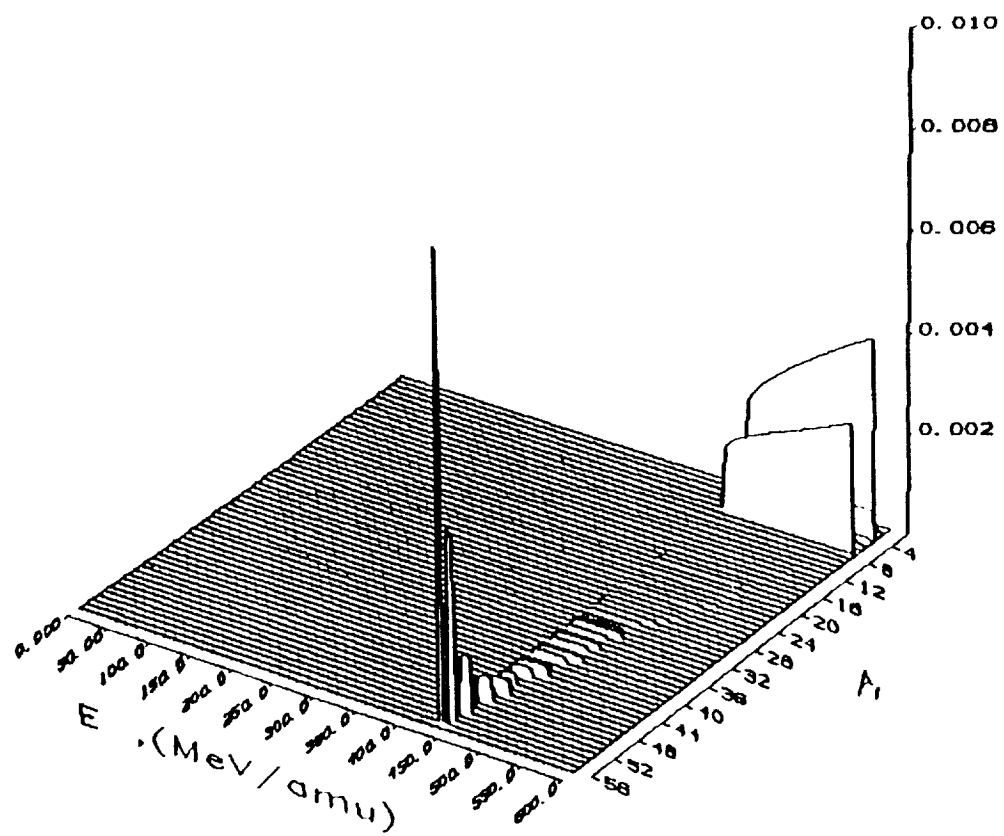


Figure 1.H. All terms perturbation solution at a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

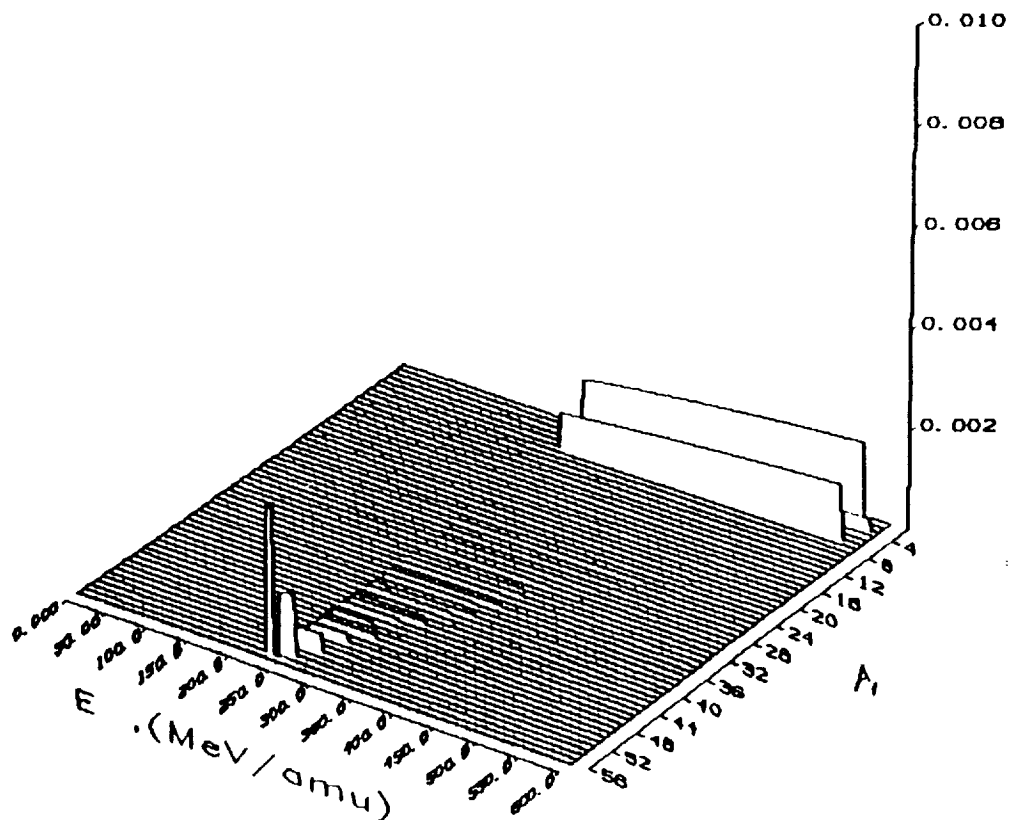


Figure 2.A. 1-st term nonperturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

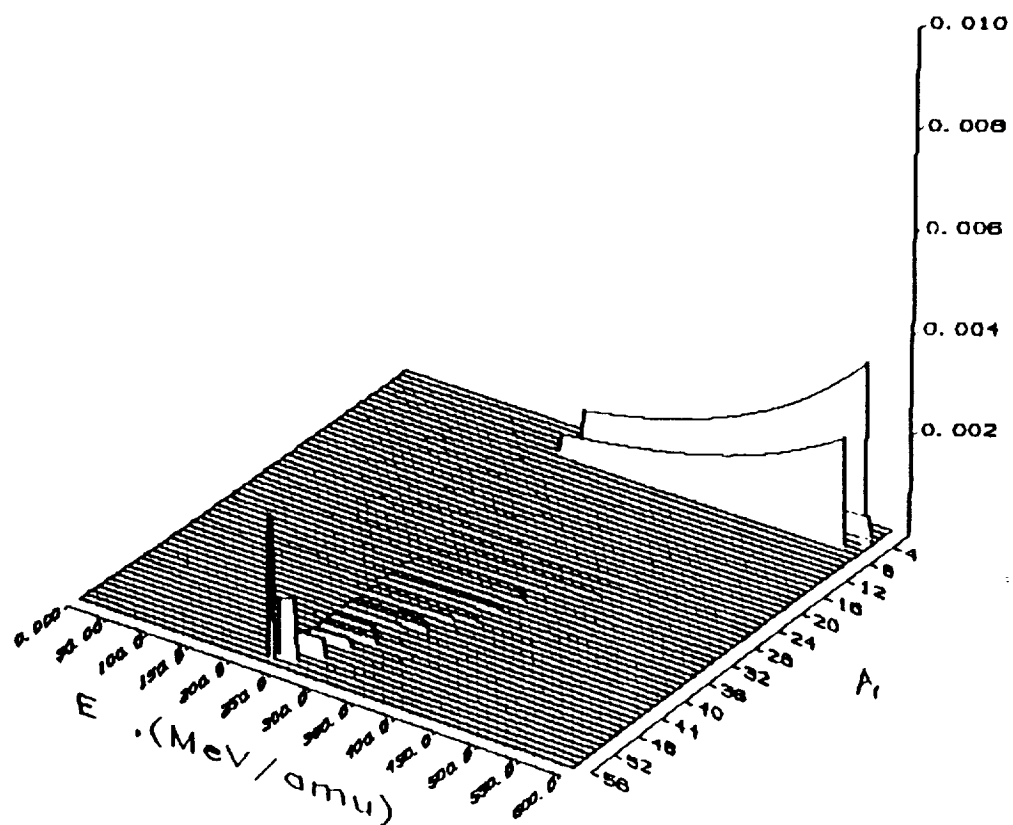


Figure 2.B. 1-st term perturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

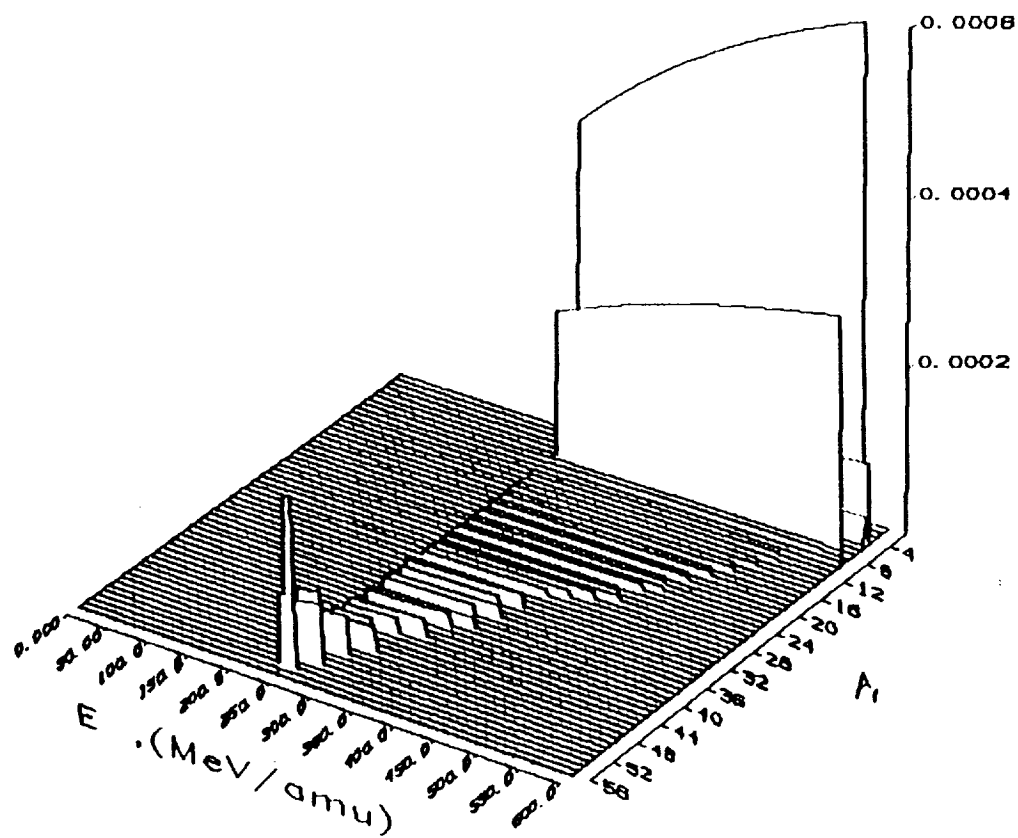


Figure 2.C. 2-nd term nonperturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

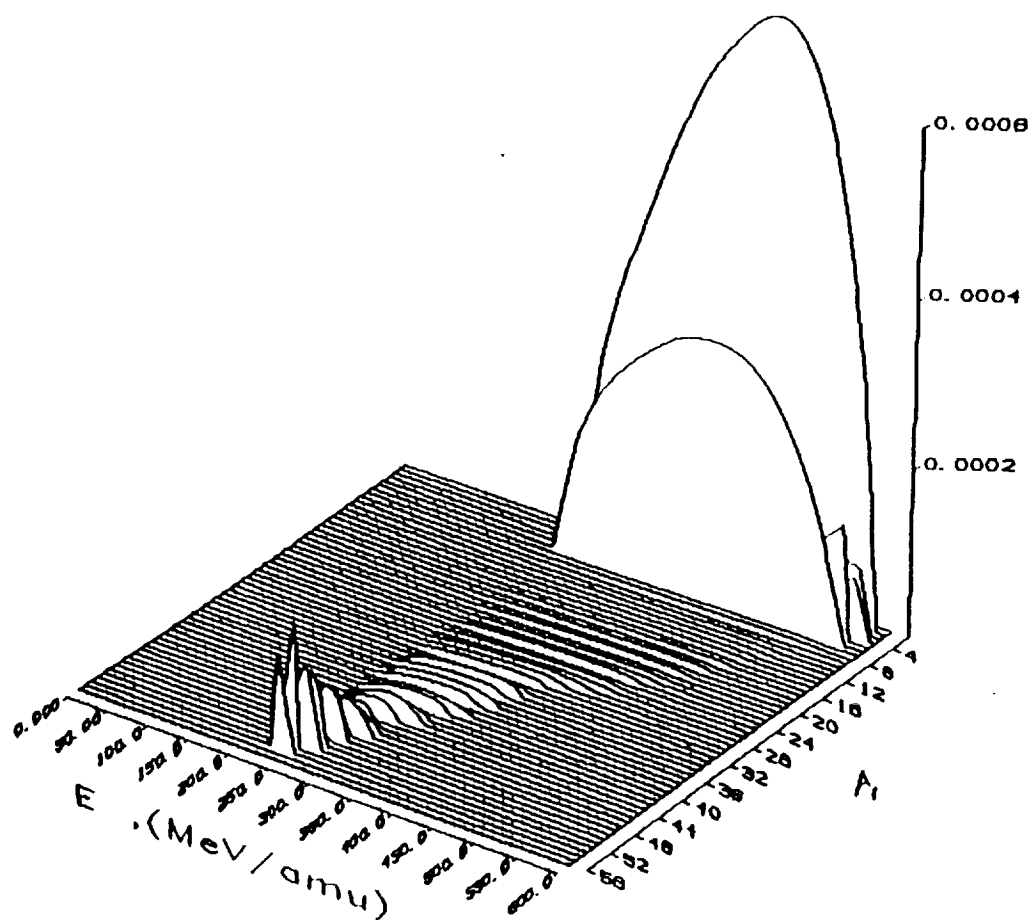


Figure 2.D. 2-nd term perturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

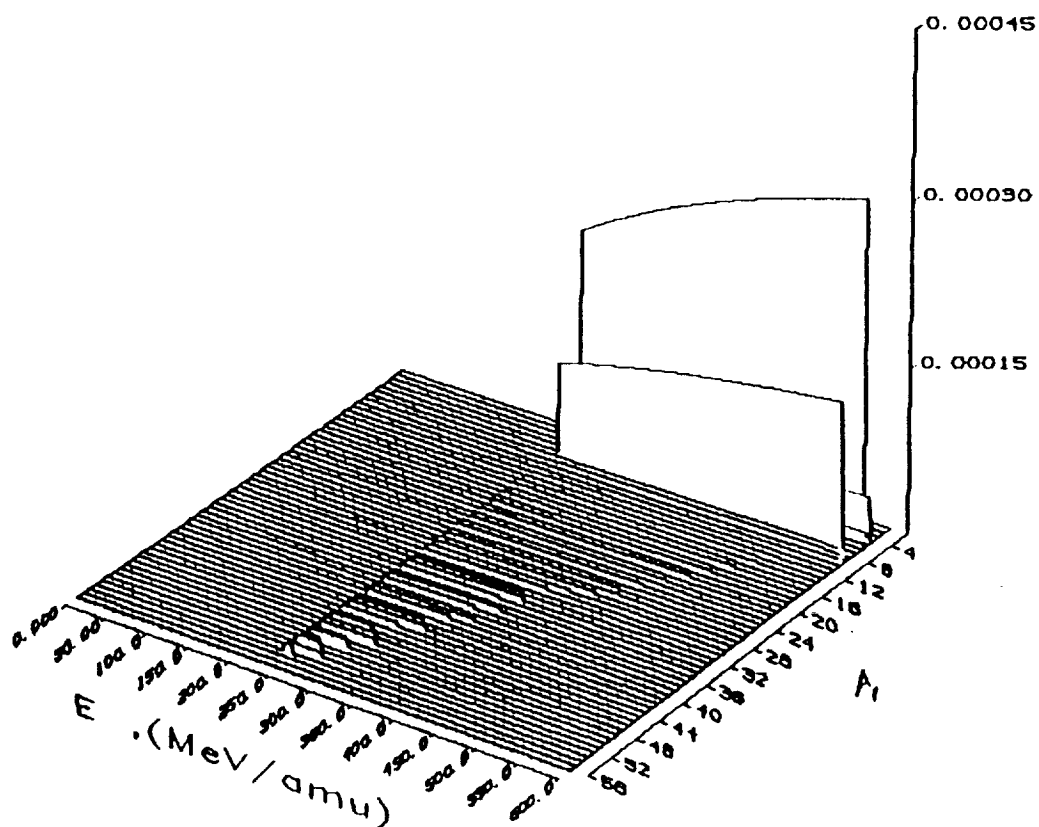


Figure 2.E. 3-rd term perturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

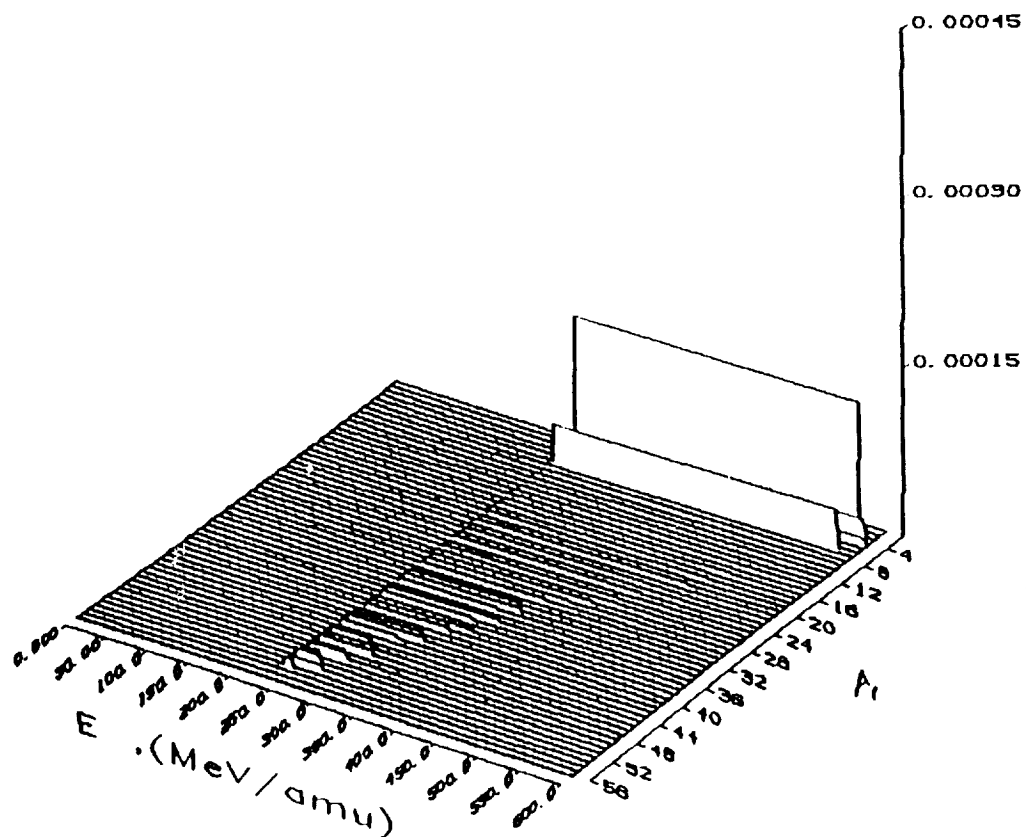


Figure 2.F. 3-rd term perturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

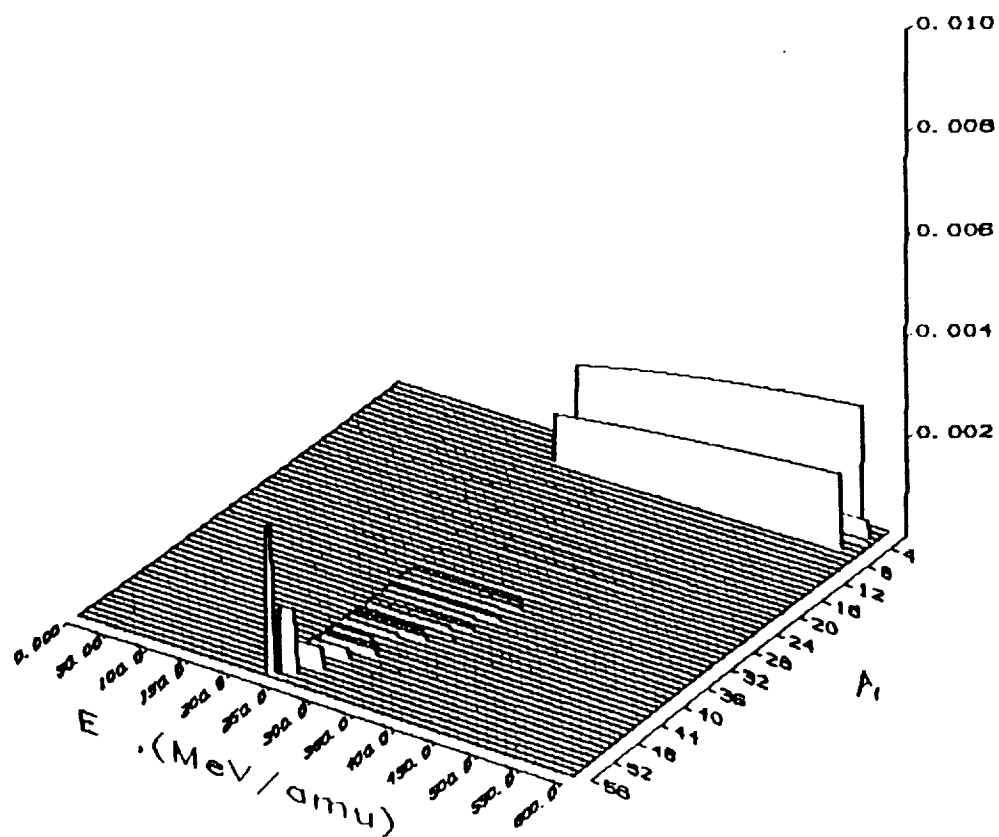


Figure 2.G. All terms nonperturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

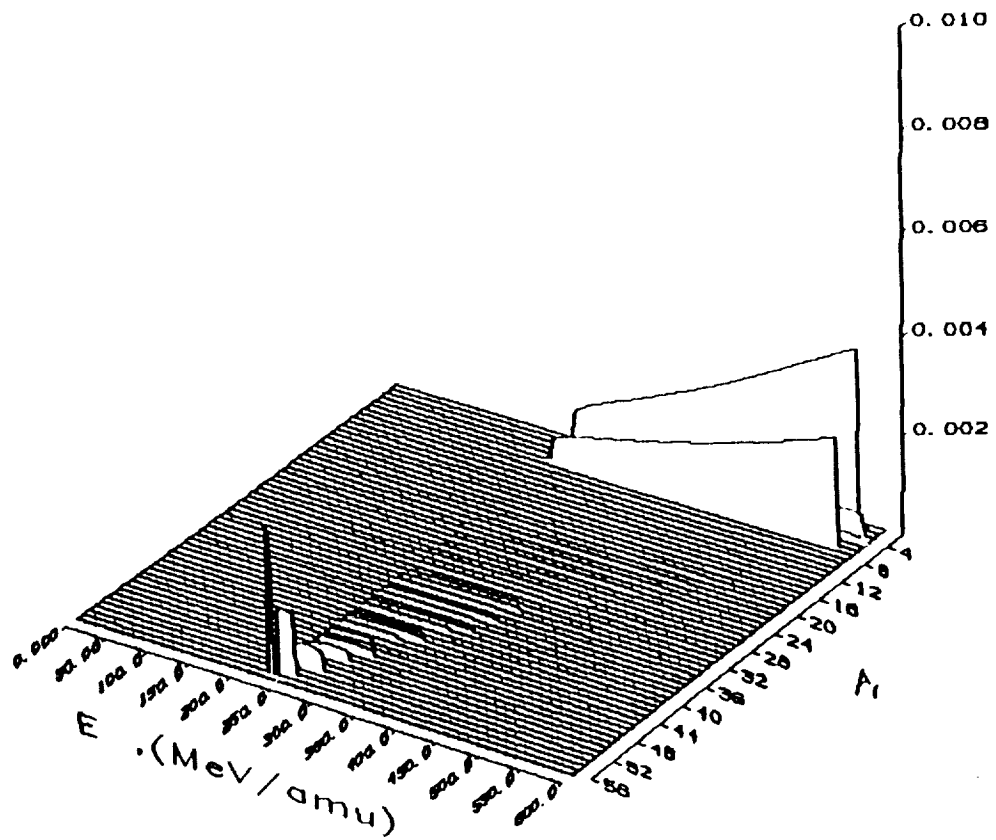


Figure 2.H. All terms perturbation solution at a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

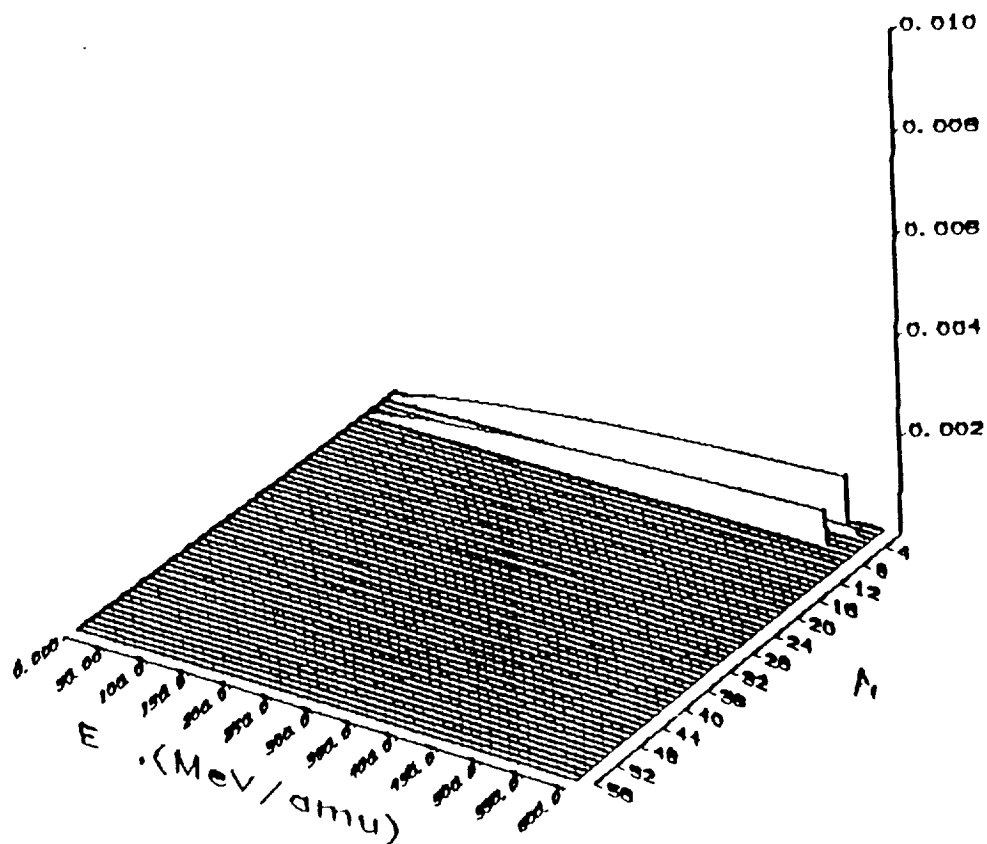


Figure 3.A. 1-st term nonperturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

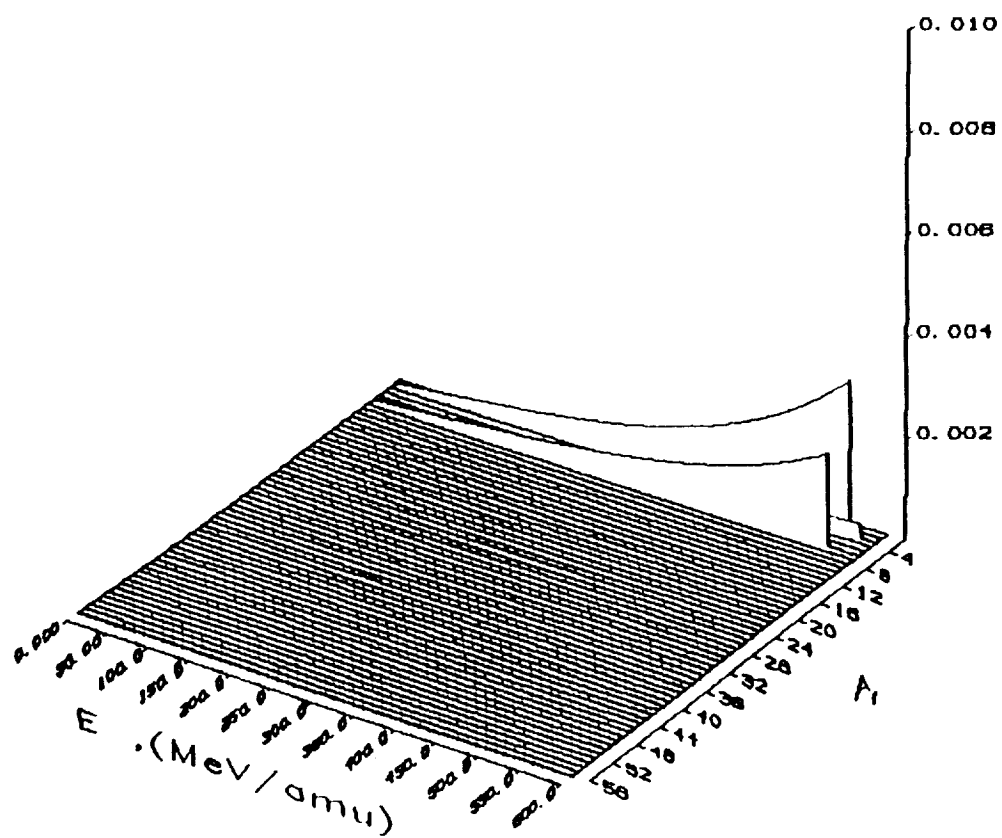


Figure 3.B. 1-st term perturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

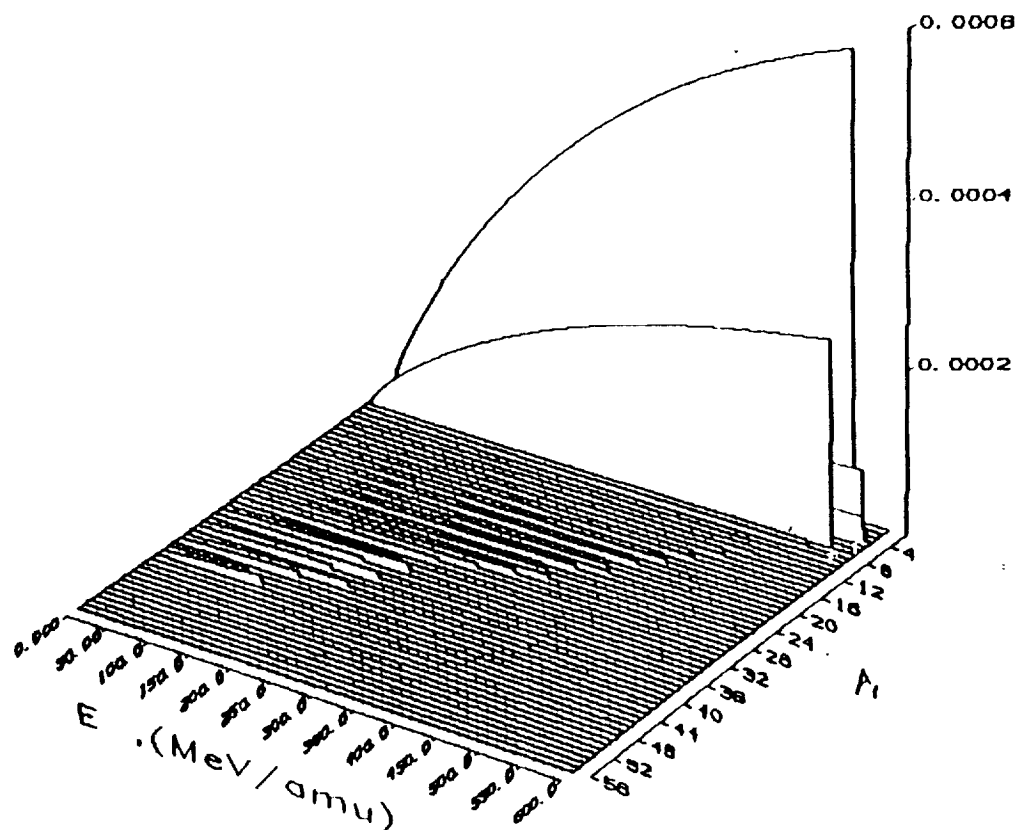


Figure 3.C. 2-nd term nonperturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

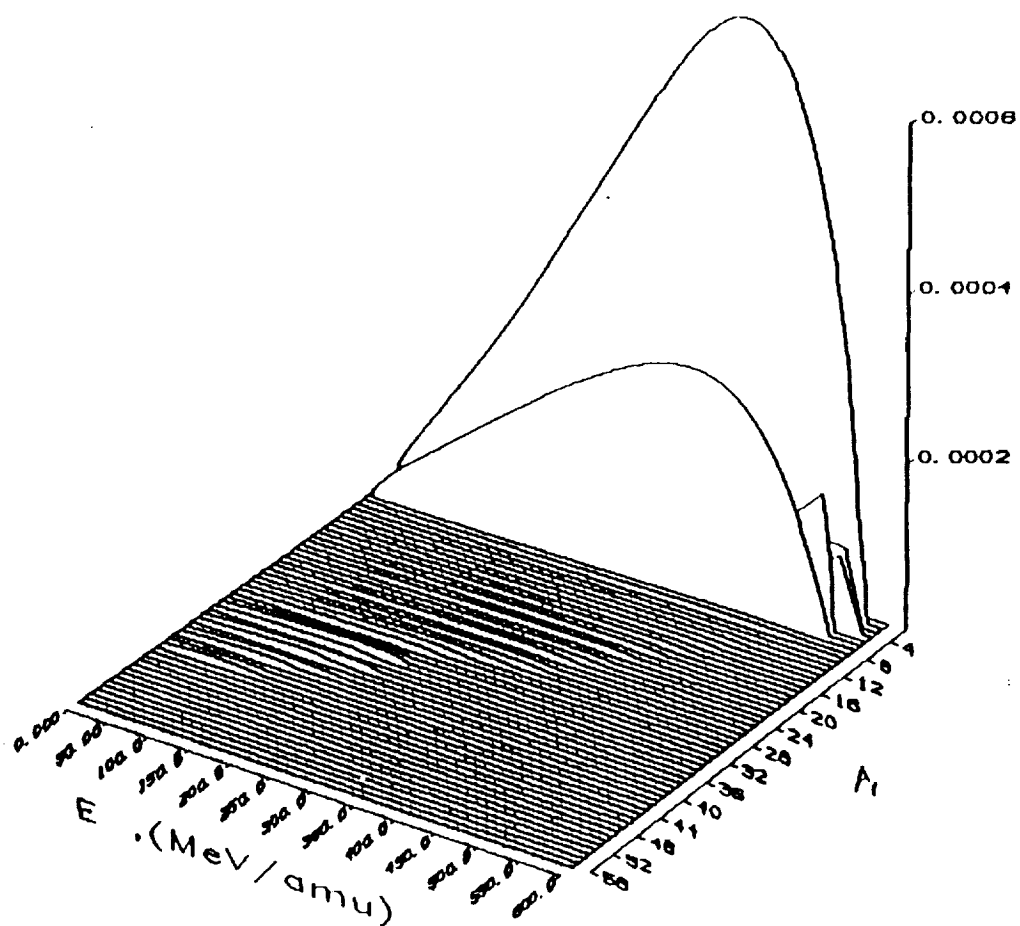


Figure 3.D. 2-nd term perturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

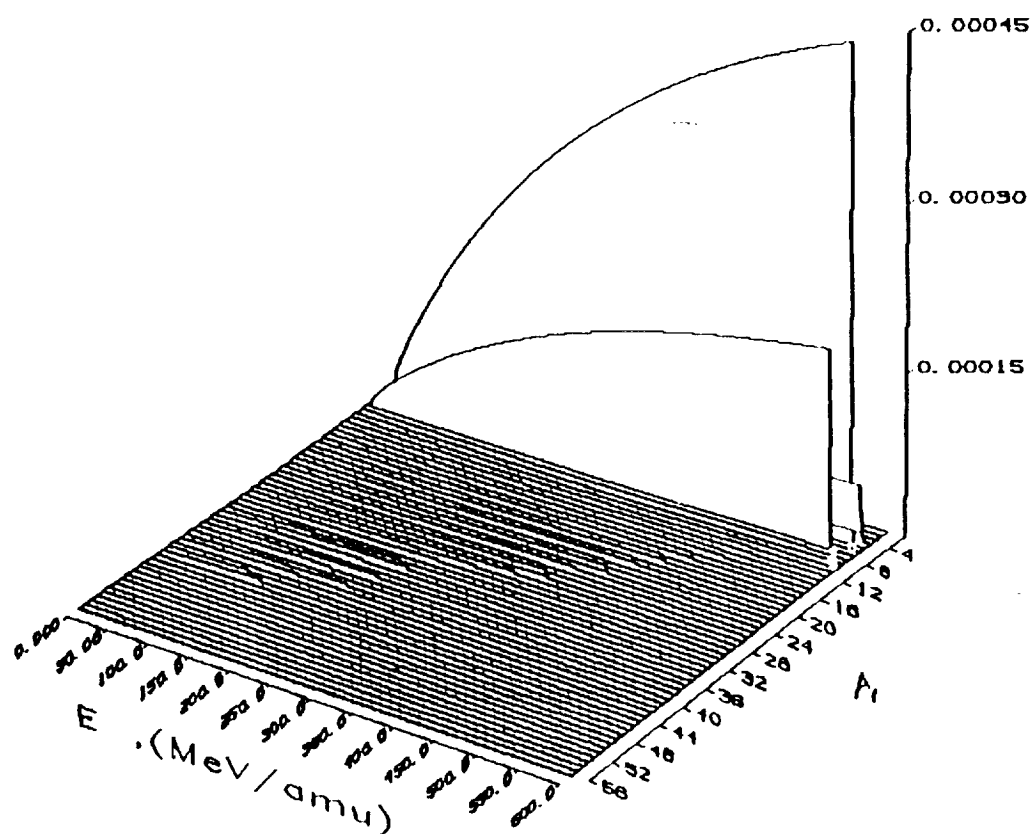


Figure 3.E. 3-rd term nonperturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

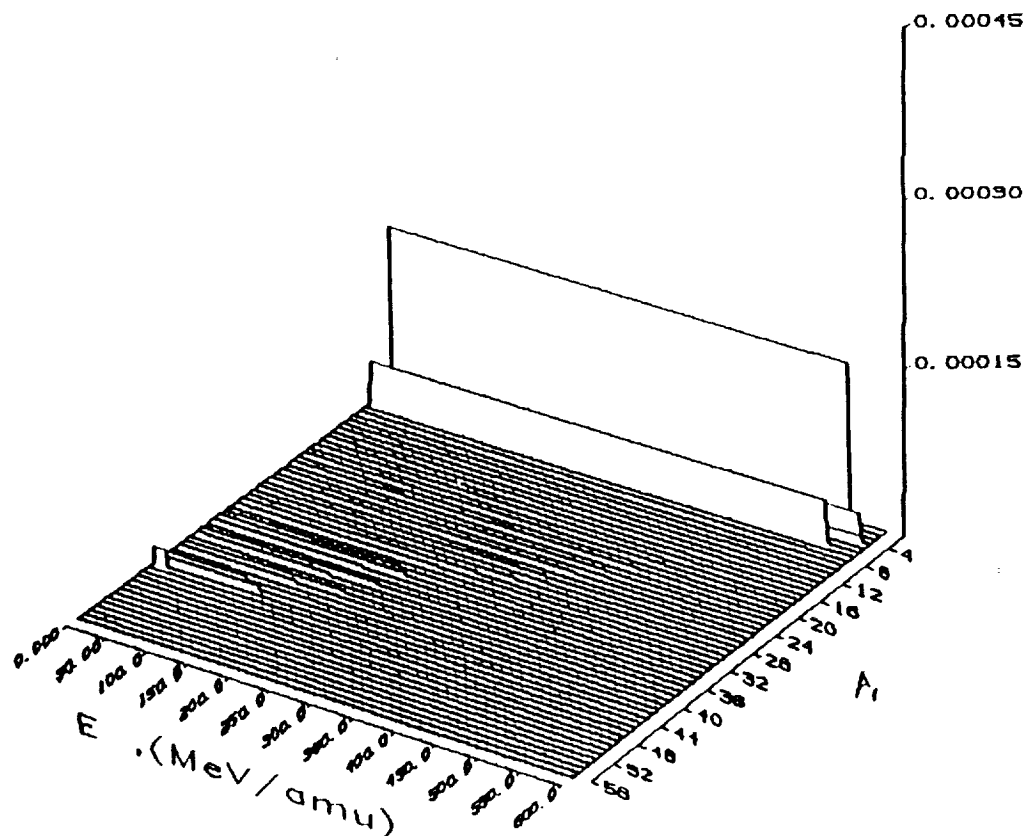


Figure 3.F. 3-rd term perturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

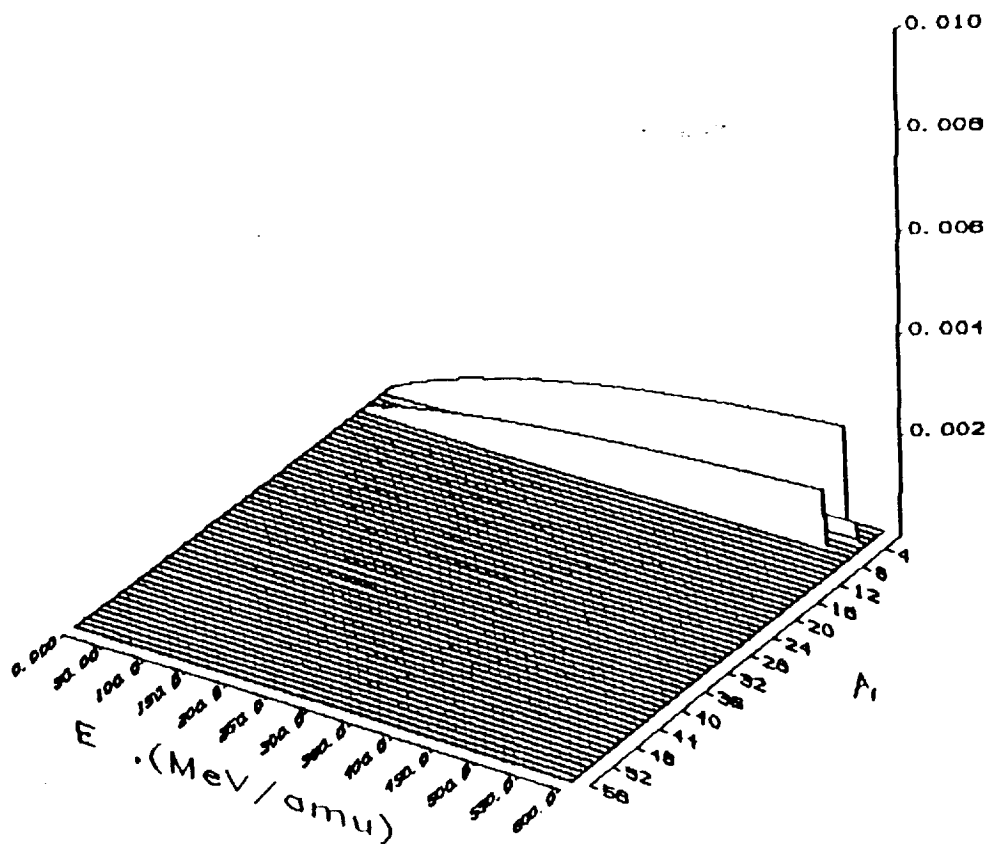


Figure 3.G. All terms nonperturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

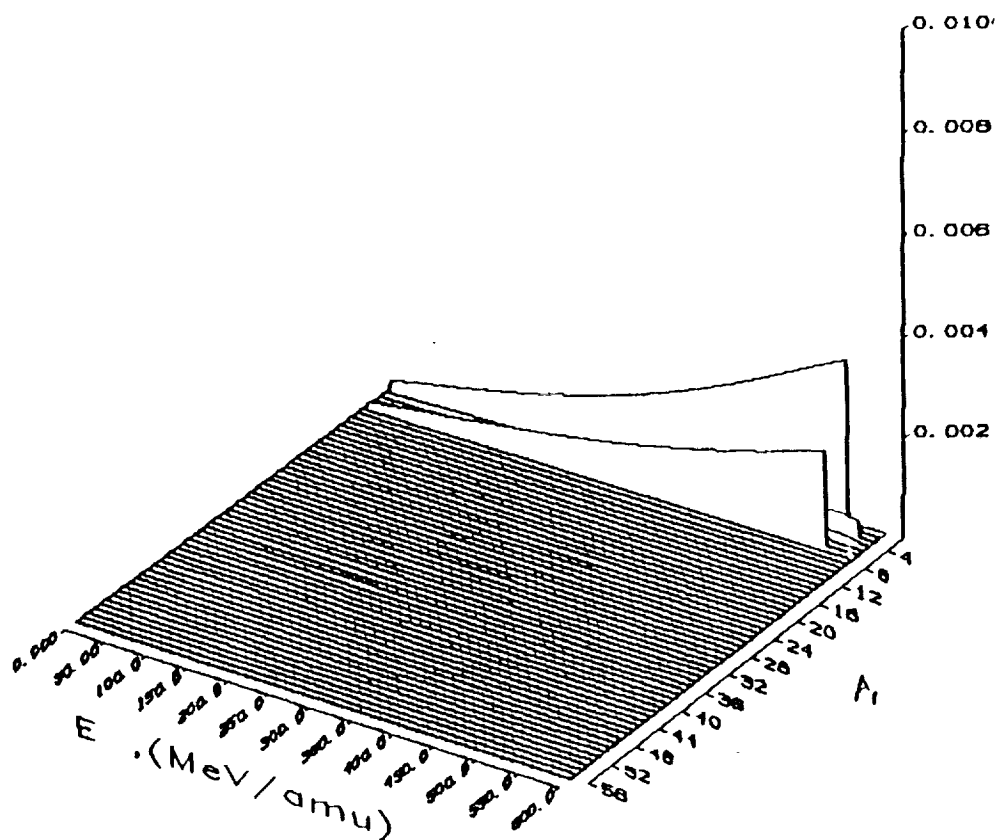


Figure 3.H. All terms perturbation solution for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.

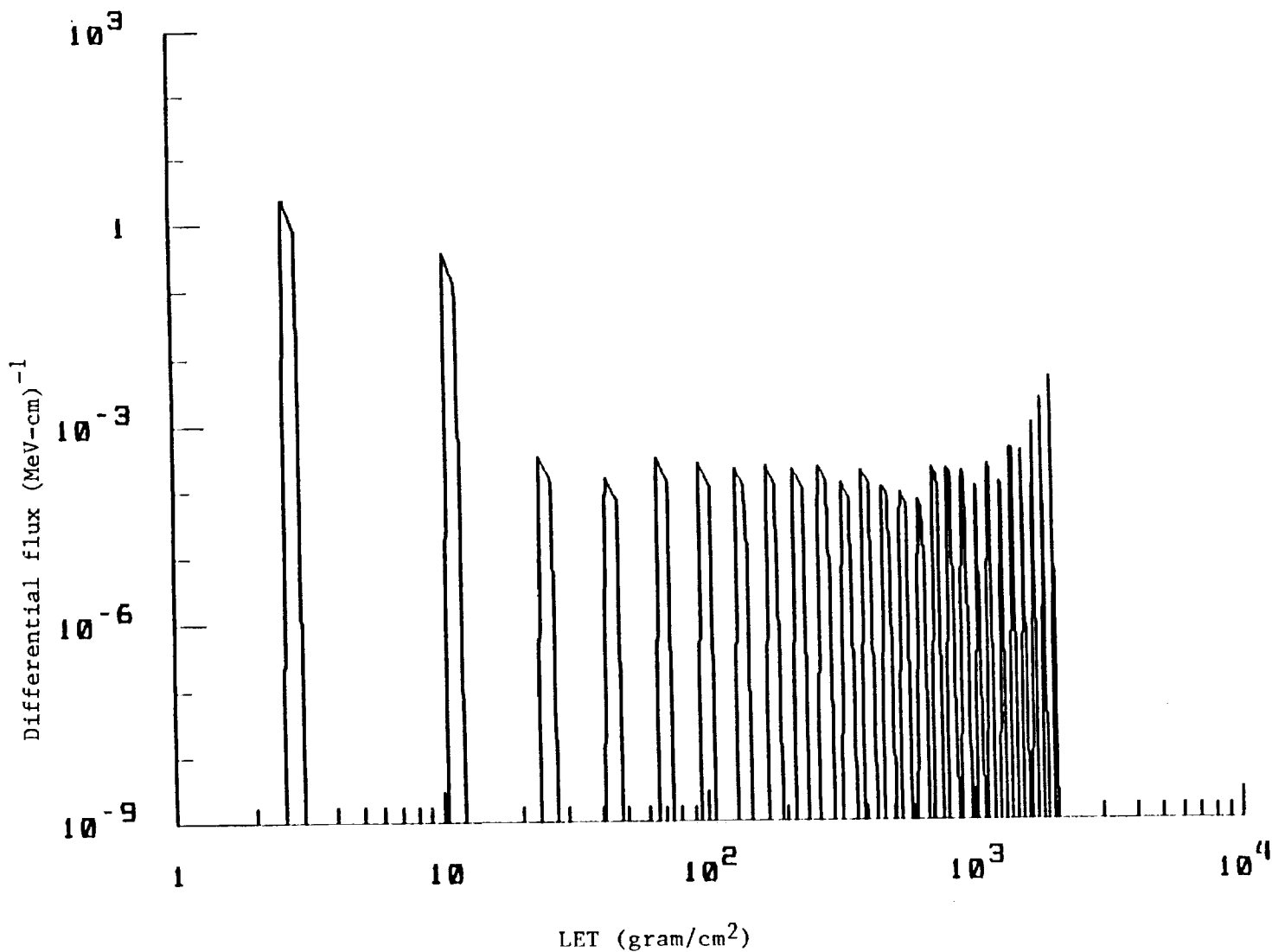


Figure 4.A. Differential LET spectrum for a depth of 5 cm of water for a 600 MeV/nucleon Iron projectile.

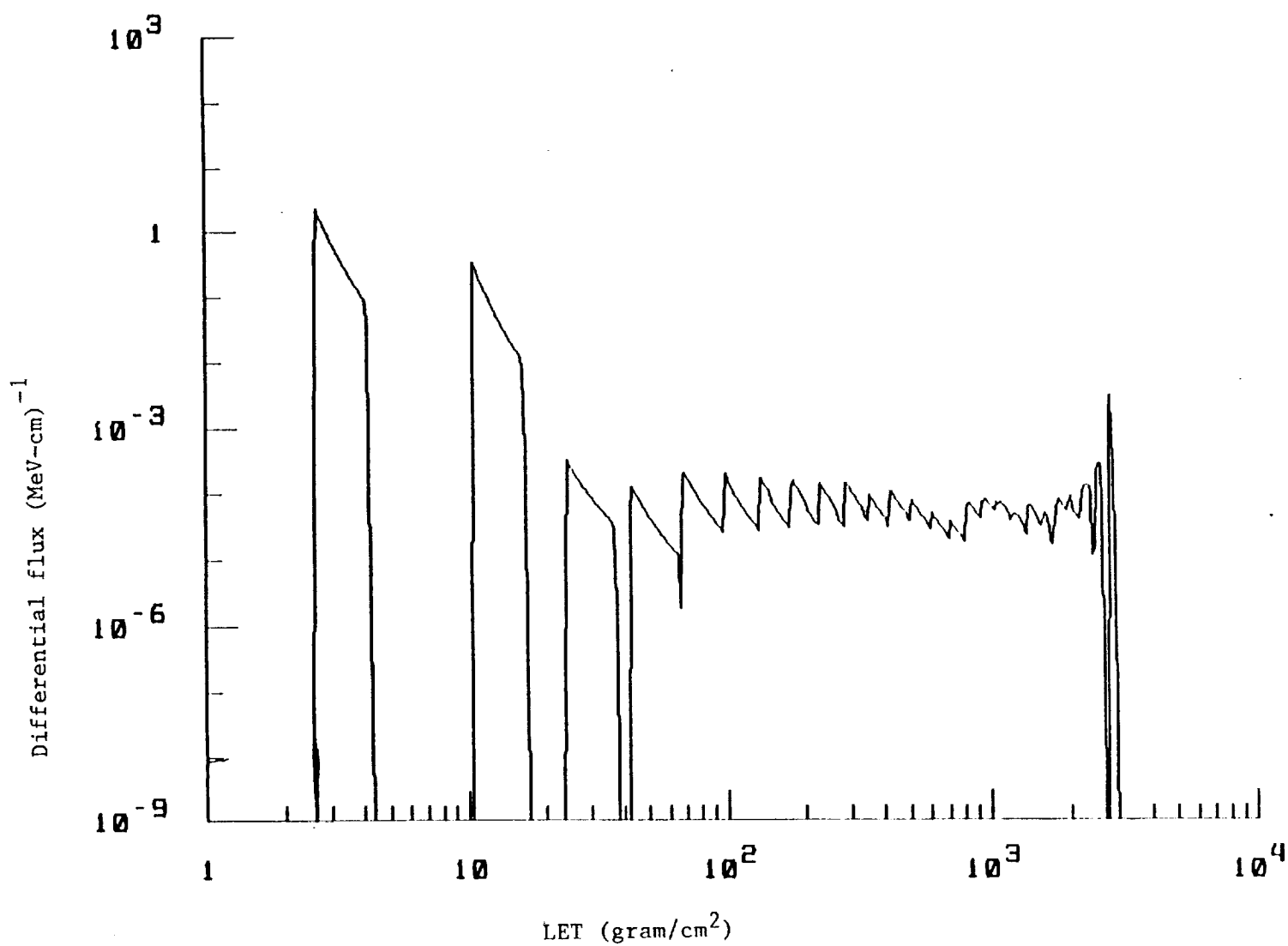


Figure 4.B. Differential LET spectrum for a depth of 10 cm of water for a 600 MeV/nucleon Iron projectile.

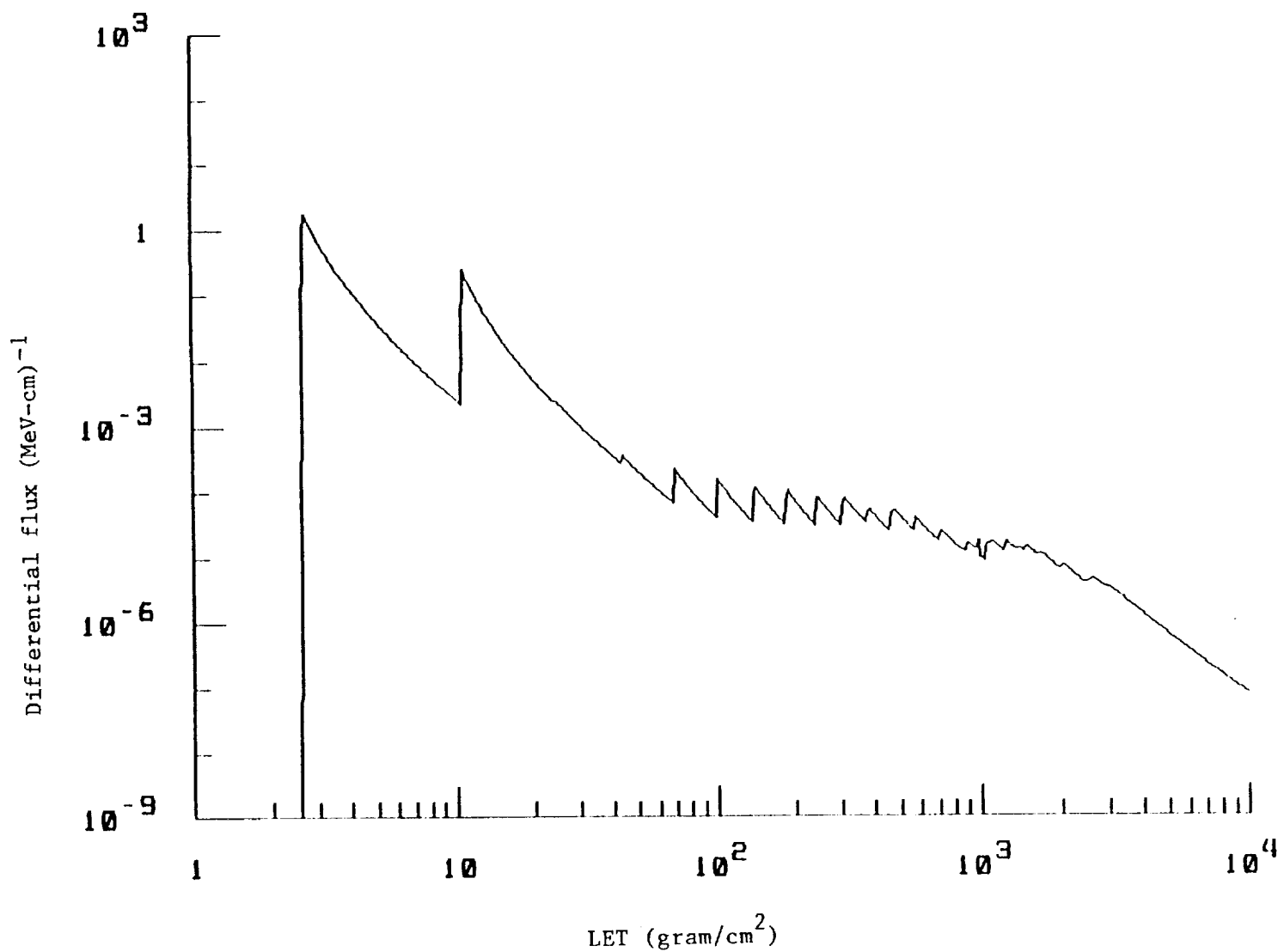


Figure 4.C. Differential LET spectrum for a depth of 15 cm of water for a 600 MeV/nucleon Iron projectile.